

# Calcul parallèle et simulation moléculaire d'adsorption dans les matériaux carbonés

**"Parallel computing and adsorption simulation  
through the carbon-based materials"**

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**27e journée du projet CASCIMODOT  
IRD, 5, rue du carbone (2 sur le plan, case F2) Université d'Orléans**



11 décembre 2017

## 1 Short presentation of ICMN formerly known as CRMD

## 2 Problem statement

- What are the micropollutants?
  - What is the adsorption process of the micro-pollutants?
  - What is the most appropriate method in modeling of the adsorption phenomenon?

### 3 Molecular simulation : Grand Canonical Monte Carlo (GCMC)

- GCMC algorithm
  - Where is the bottleneck of GCMC computations?

## 4 Parallel algorithm paradigms

- First paradigm: Energy subroutine is only parallelized
  - Second paradigm: Virtual volume concept
  - Speedup and efficiency
  - CO<sub>2</sub> adsorption outcomes

## 5 Conclusions and outlooks

- ## ■ Conclusions



## ■ Outlooks

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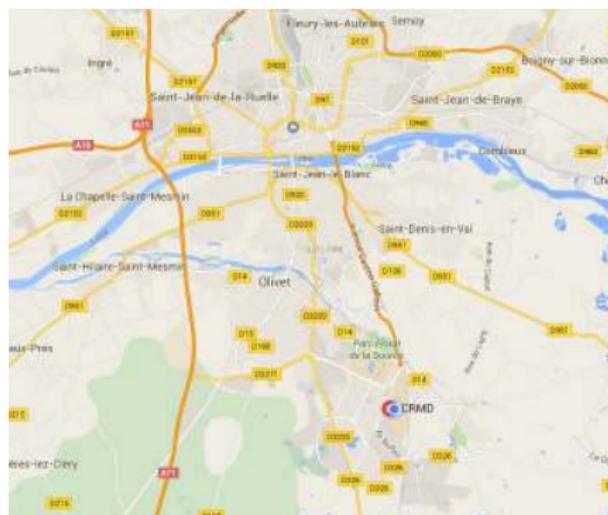
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# Présentation de l'ICMN ex CRMD

- ICMN - UMR7374 (Institut de Physique)
- 27 permanents (PR, DR, MCF, MCF-HDR, IR, IE) et 10 non-permanents (doctorants et post-doctorants).



(a)



(b)

**Figure:** Plan du campus CNRS et Polytech Orléans.

# Présentation de l'ICMN ex CRMD

Équipes de recherche, <http://www.icmn.cnrs-orleans.fr/>

## 1 Matériaux Nanostructurés et Confinés

- i Thermodynamique et structure à l'échelle nanométrique,
- ii Auto-organisation ou structuration,
- iii Dynamique dans les systèmes confinés.



## 2 Carbone fonctionnels-Environnement-Biomatériaux

- i Élaboration du matériau carboné fonctionnalisé (Carbone fonctionnels),
- ii Intégration des carbones dans des systèmes ou procédés (Environnement),
- iii Étude de la réactivité interfaciale et des propriétés physico-chimiques (Biomatériaux).



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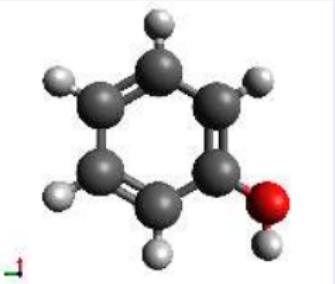


# What are the micropollutants?

Main micropollutants: Nanoparticles, Biphenol, Phenol, Phenol, Phthalate ...



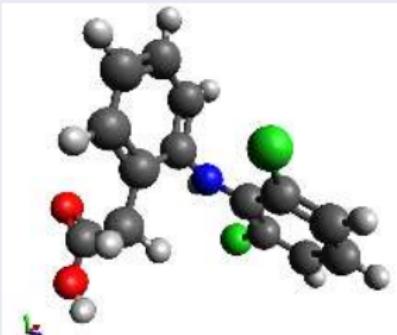
(a) Biphenol (C<sub>12</sub>H<sub>10</sub>O<sub>2</sub>)



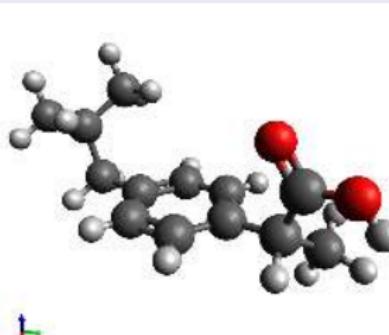
(b) Phenol (C<sub>6</sub>H<sub>6</sub>O)



(c) Phthalate (C<sub>8</sub>H<sub>4</sub>O<sub>4</sub>)



(d) Diclofenac (C<sub>14</sub>H<sub>11</sub>Cl<sub>2</sub>NO<sub>2</sub>)



(e) Ibuprofen C<sub>13</sub>H<sub>18</sub>O<sub>2</sub>

# What are the micropollutants?

## Problem statement

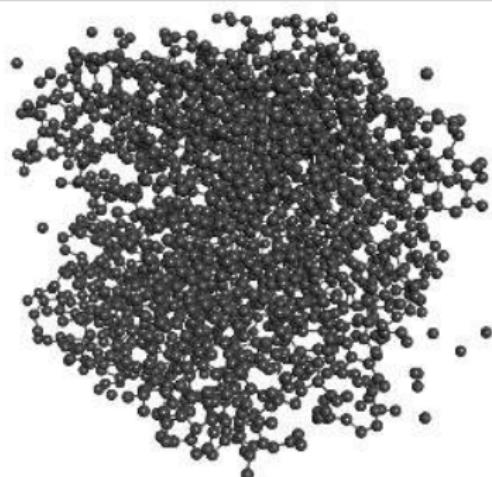
### Major issues about the micropollutants

- 1 The micropollutants are the most challenge for the environment.
- 2 They can be readily found out in the drinking water.
- 3 The EU strengthens the restrictions on the micropollutants concentration in the drinking water.

## Remedies:

- 1 Optimizing existing procedures,
- 2 **Additional treatment procedures.**

- 1 Ozonation: ozone is a powerful oxidizing agent that degrades chemical substances in gas and liquid mixtures,
- 2 Advanced oxidation processes: adding hydrogen peroxide and ultraviolet light to ozone to intensify the oxidation process.
- 3 **Adsorption on granular activated carbon:** the porous structure facilitates adsorption of a wide range of micropollutants.



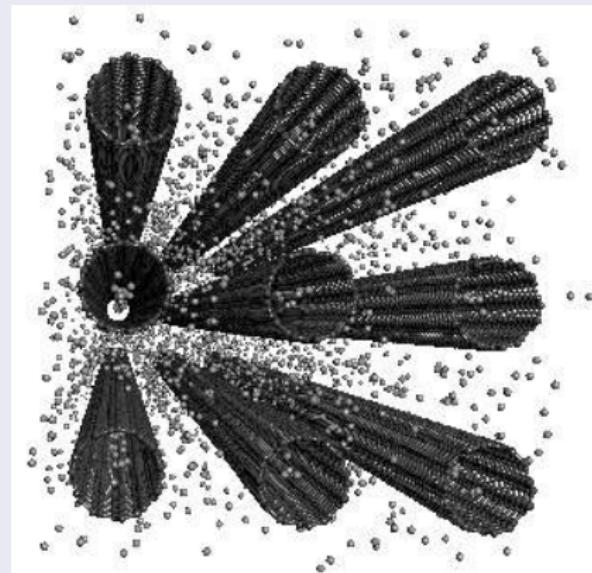
(a) Activated carbon [Pikunic et al., 2003]

# What is the adsorption process of the micro-pollutants?

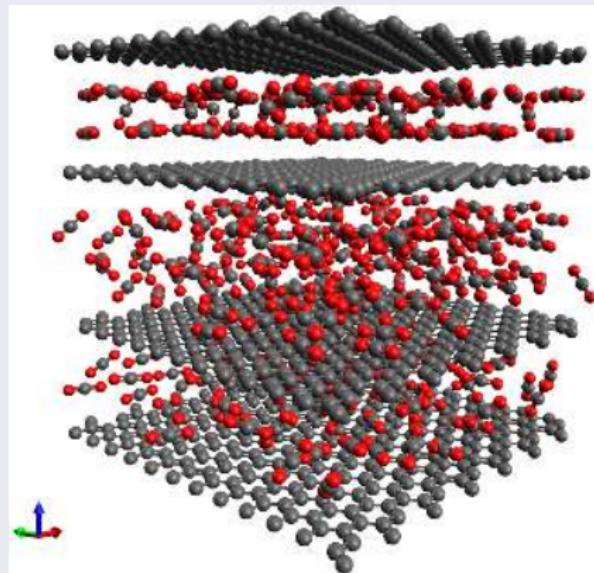
Main definition

**Adsorption is the adhesion of atoms, ions, or molecules from a gas, liquid, or dissolved solid to a surface.**

(a) H<sub>2</sub> adsorption in SWCNT [Kouetcha et al., 2015]



(b) CO<sub>2</sub> adsorption illustration



# Physisorption (physical adsorption) and Chemisorption (chemical adsorption)

## Adsorption types

- **Physisorption** or so-called physical adsorption, is a process in which the electronic structure of the atom or molecule is mainly perturbed upon adsorption,
- **Chemisorption** or so-called chemical adsorption involves a chemical reaction between the surface and the adsorbate.

## Physical adsorption modeling

- The physical adsorption can be handled via the
  - 1 statistical mechanics,
  - 2 ensembles of the statistical mechanics (Grand Canonical ensemble)
- Physical adsorption using the Grand Canonical ensemble assumes given values for the **chemical potential, temperature and volume**.
- The **guest molecules density and their positions, adsorption heat and pressure** can be computed.

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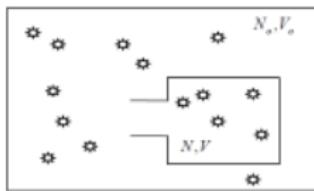
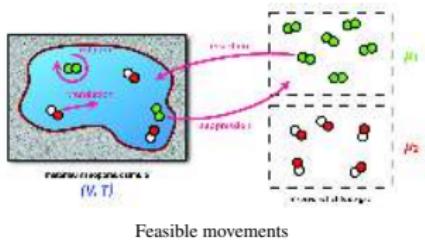
### 5 Conclusions and outlooks

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# Molecular simulation : Grand Canonical Monte Carlo

Probability rules [Metropolis et al., 1953]



## ■ Creation

$$P_{\text{acc}}(\mathbf{r}^N \rightarrow \mathbf{r}^{N+1}) = \min \left( 1, \frac{V \exp(\beta \mu)}{(N+1) \Lambda^3} \times \exp \left[ -\beta \left( U(\mathbf{r}^{N+1}) - U(\mathbf{r}^N) \right) \right] \times \frac{P_{\text{gen}}(\mathbf{r}^{N+1} \rightarrow \mathbf{r}^N)}{P_{\text{gen}}(\mathbf{r}^N \rightarrow \mathbf{r}^{N+1})} \right)$$

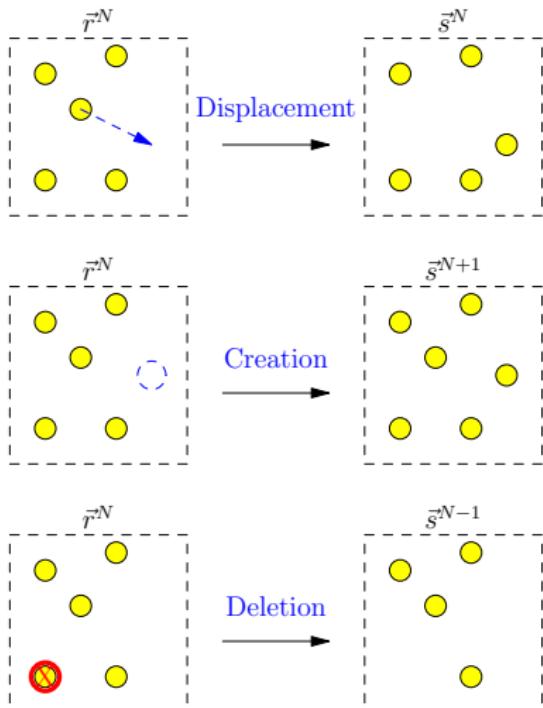
## ■ Deletion

$$P_{\text{acc}}(\mathbf{r}^N \rightarrow \mathbf{r}^{N-1}) = \min \left( 1, \frac{N \Lambda^3}{V \exp(\beta \mu)} \times \exp \left[ -\beta \left( U(\mathbf{r}^{N-1}) - U(\mathbf{r}^N) \right) \right] \times \frac{P_{\text{gen}}(\mathbf{r}^{N-1} \rightarrow \mathbf{r}^N)}{P_{\text{gen}}(\mathbf{r}^N \rightarrow \mathbf{r}^{N-1})} \right)$$

## ■ Displacement

$$P_{\text{acc}}(\mathbf{r}^N \rightarrow \mathbf{r}^{N-1}) = \min \left( 1, \exp \left[ -\beta \left( U(\mathbf{r}^{N-1}) - U(\mathbf{r}^N) \right) \right] \times \frac{P_{\text{gen}}(\mathbf{r}^{N-1} \rightarrow \mathbf{r}^N)}{P_{\text{gen}}(\mathbf{r}^N \rightarrow \mathbf{r}^{N-1})} \right)$$

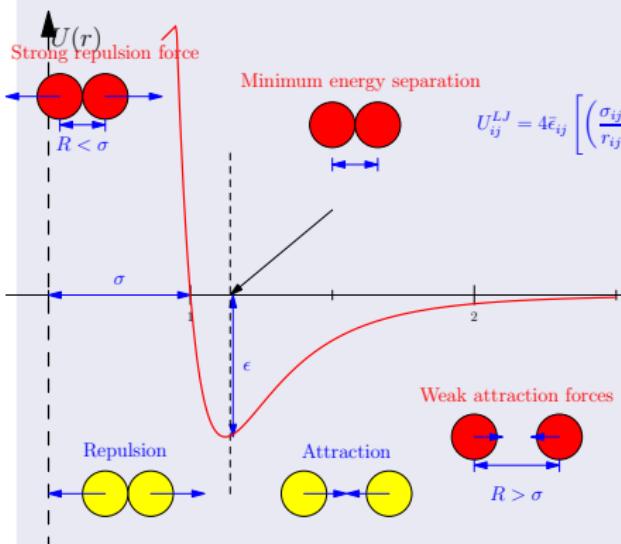
# Molecular simulation : GCMC kernel



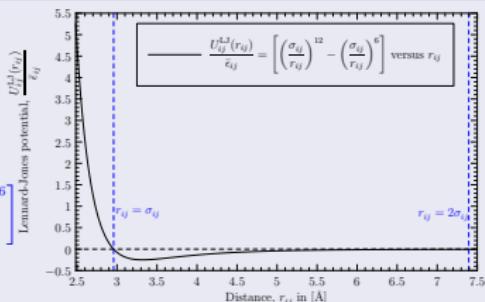
**(a)** GCMC statistical engine [Allen and Tildesley, 1989; Frenkel and Smit, 2002; Ramézani and Chuta, 2014]

## Grand Canonical Monte Carlo (GCMC)

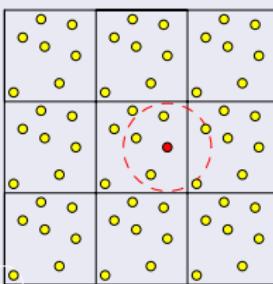
## Van der Waals Potential energy illustration



(a) Lennard Jones curve illustration [Crowell and Brown, 1982; Wang and Johnson, 1998]

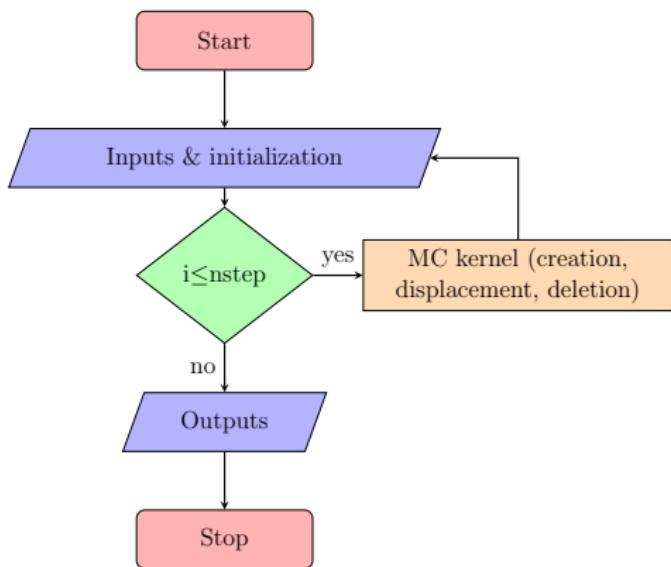


(a) LJ curve of H<sub>2</sub>



**(b)** Cut-off sphere illustration

# Grand Canonical Monte Carlo (GCMC): Basic flowchart

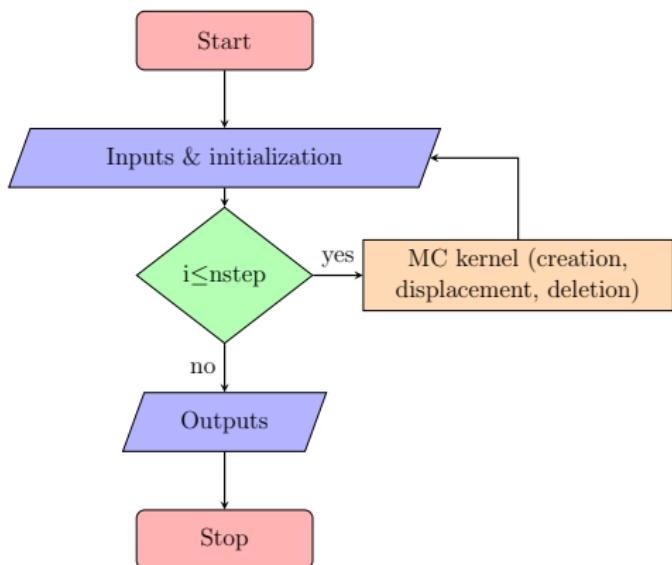


(a) Simple flowchart of GCMC [Chuta, 2013]

## Why does one need the supercomputing?

- 1 Monte Carlo method needs at least  $10^3$  iterations per host atom for so-called rigid molecules (one-point molecule assumption),
- 2 This gets worse when the non-rigid molecules are considered and iteration no. must be greater than  $10^6$ .
- 3 The adsorption curves will undertake various chemical potentials and it means that it is required to perform the simulations for every single point in the plot (iteration no. = $50 \times 10^6$  per host atom).

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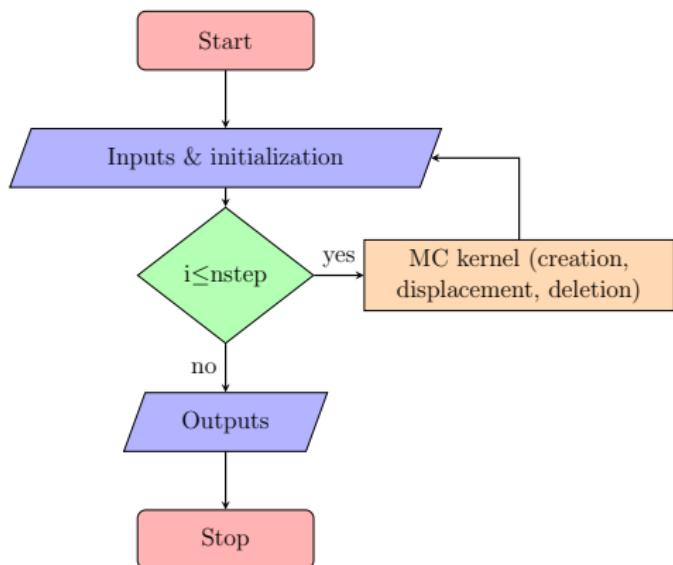


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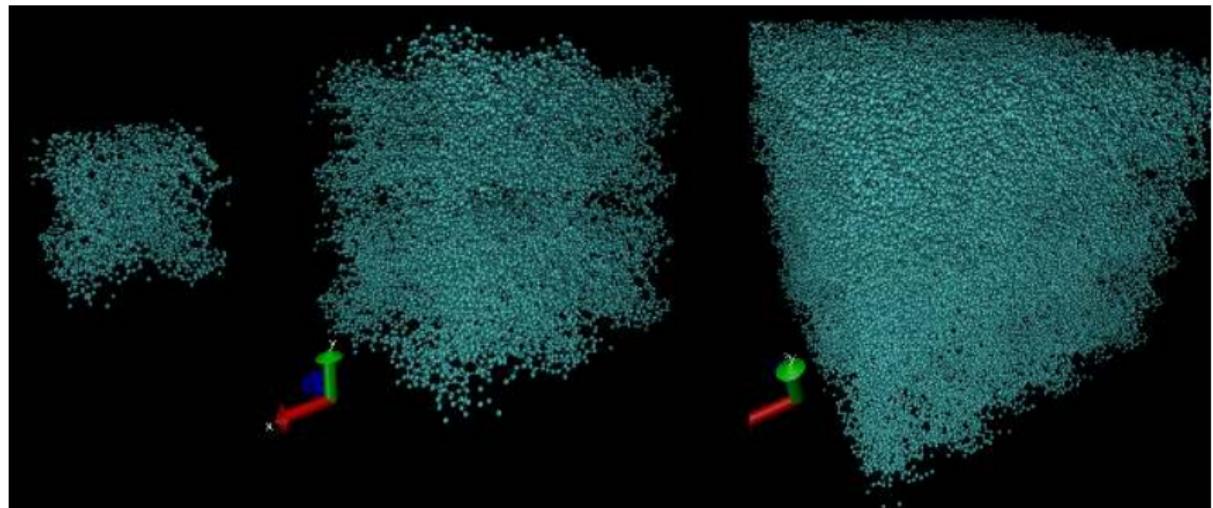
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## Grand Canonical Monte Carlo (GCMC)

## Highly disordered structures



**(a)** Size effect (from  $30 \times 30 \times 30$  to  $90 \times 80 \times 90$  Å)

<b>Size</b>	$30 \times 30 \times 30$	$60 \times 60 \times 60$	$90 \times 90 \times 90$	$120 \times 120 \times 120$	$240 \times 240 \times 240$	$360 \times 360 \times 360$
<b>No. of atoms</b>	2130	17040	57510	136320	1090560	3680640

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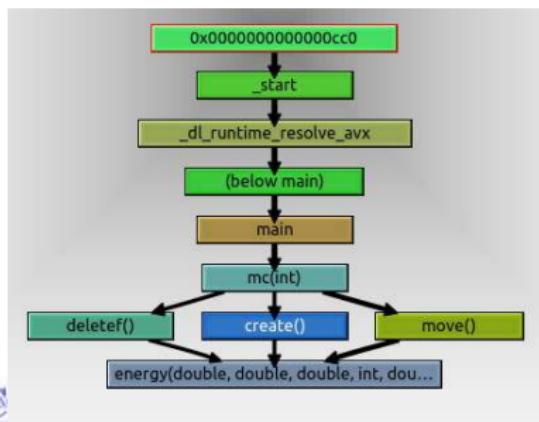


# Grand Canonical Monte Carlo (GCMC) and its bottleneck

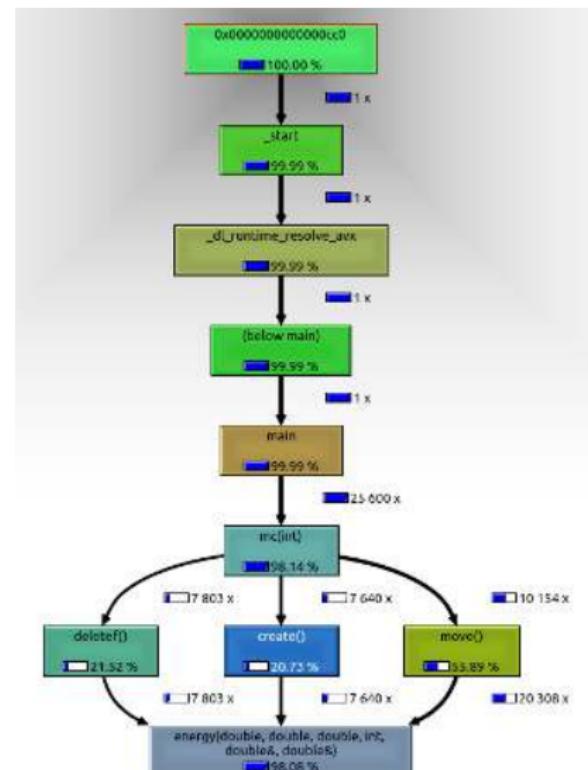
Main goals and single program profiling of the serial GCMC code (GNU compilers and valgrind profiler)

## Main goals

- Code portability [Stroustrup, 2013],
- Code parallelism and scalability,
- Code flexibility.



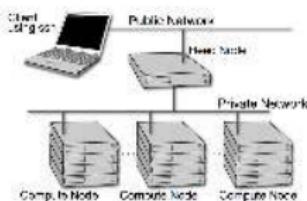
(a) Compact graph of GCMC code



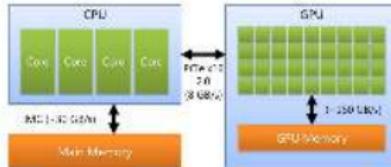
(b) Normal graph of GCMC code.

# Parallel computing (OpenMP/MPI/CUDA)

## Message Passing Interface (MPI-3)



(a) CPU computing



(b) GPU computing

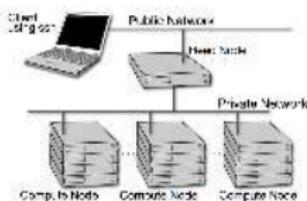
- MPI programming is applied for the parallel computations herein (MPI-3) [Gropp et al., 2014a,b; Karniadakis and Kirby, 2003; Snir, 1998],
- GNU GCC compilers (gcc 5.3.0) and open MPI 1.10.2 are mainly used to do the experiments,
- Parallel computations have been carried out in the CCSC cluster in France (<http://cascimodot.fdpoisson.fr/ccsc>).
- Two different Parallel MPI implementations have been taken into account:

1 Energy subroutine is solely parallelized (First paradigm)

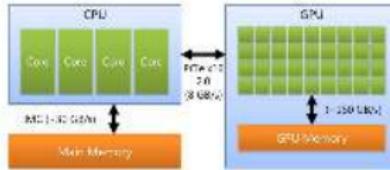
2 Virtual volumes have been created and the averaging issues of GCMC have been achieved. Monte Carlo iterations have been parallelized as a whole (Second paradigm)

# Parallel computing (OpenMP/MPI/CUDA)

## Message Passing Interface (MPI-3)



(c) CPU computing



(d) GPU computing

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1 **Energy subroutine** is solely parallelized (**First paradigm**)

2 Virtual volumes have been created and the averaging issues of GCMC have been achieved. **Monte Carlo iterations have been parallelized** as a whole (**Second paradigm**)

## Parallel computing

First paradigm: Energy subroutine is only parallelized

## First paradigm

- The energy subroutine takes 98.08% of computation cost.
  - The energy subroutine parallelization may reduce the computation runtime.

## Parallelization of energy subroutine

- The energy subroutine main loop has been distributed along the CPUs and the outcomes have been collected via the MPI collective functions (MPI\_Allreduce and MPI\_Reduce).
  - The following MPI functions have been globally applied to perform the parallel computing.
    - 1 **Basic MPI functions:** MPI\_Init, MPI\_Comm\_size, MPI\_Comm\_rank and MPI\_Finalize,
    - 2 **Additional MPI functions:** MPI\_time, MPI\_Barrier, MPI\_Allreduce and MPI\_Reduce.

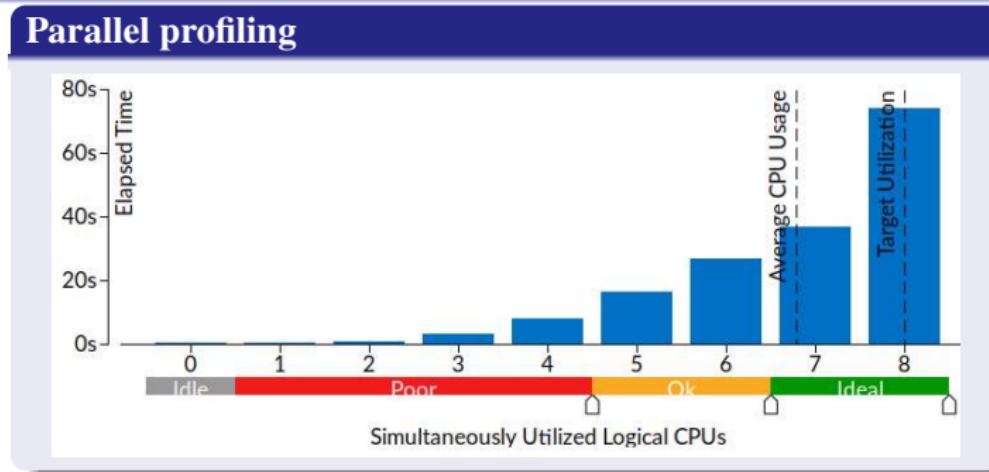
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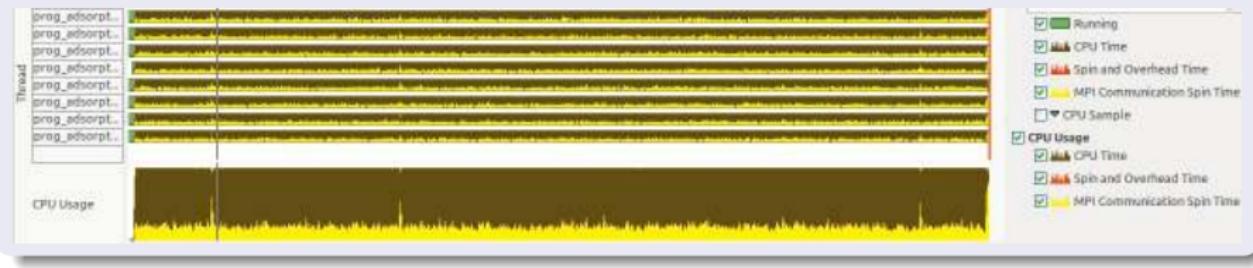
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## First paradigm

## Parallel profiling and CPU usage



## CPU usage



# Second paradigm via virtual volumes [Deublein et al., 2011]

Parallel profiling and CPU usage

## Second paradigm

- Monte Carlo computations would be performed in the virtual volumes in an independent manner,
- Every single processor achieves the Monte Carlo simulations in its corresponding virtual volume.

## Parallelization of MC iterations

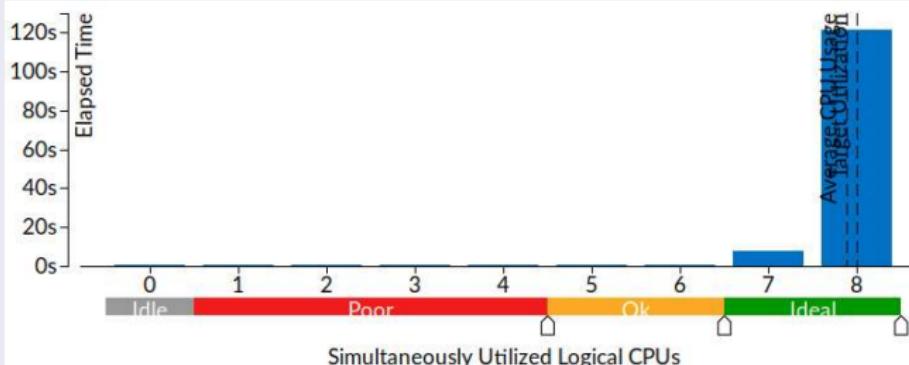
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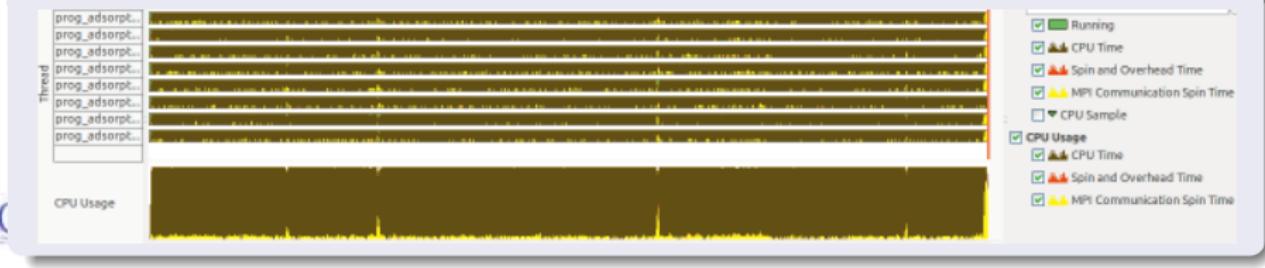
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Parallel profiling and CPU usage

## Parallel profiling

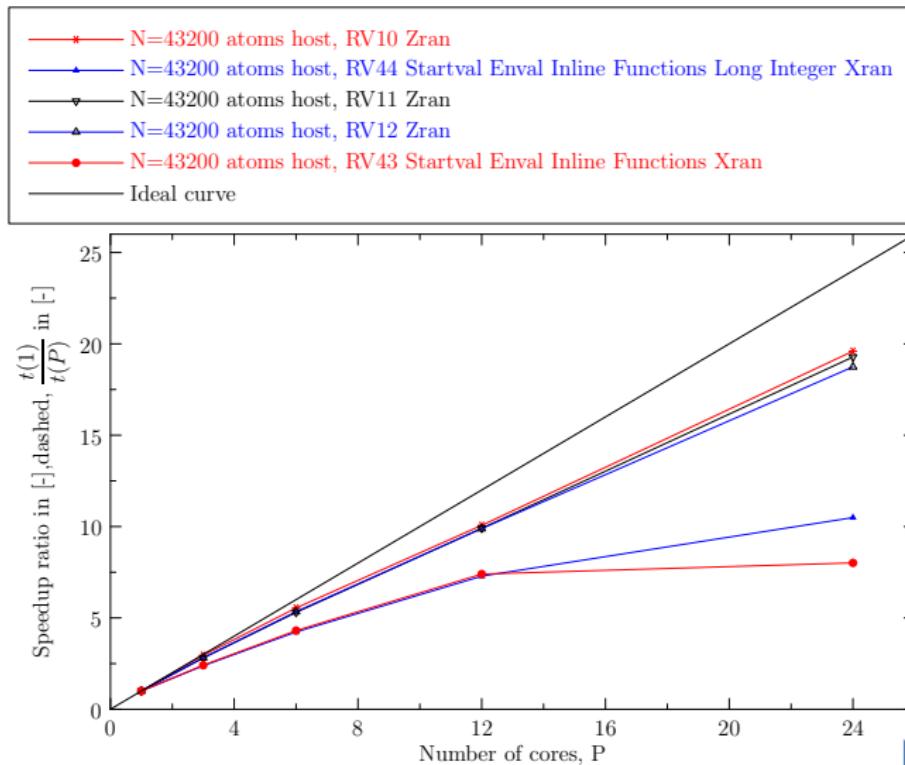


## CPU usage



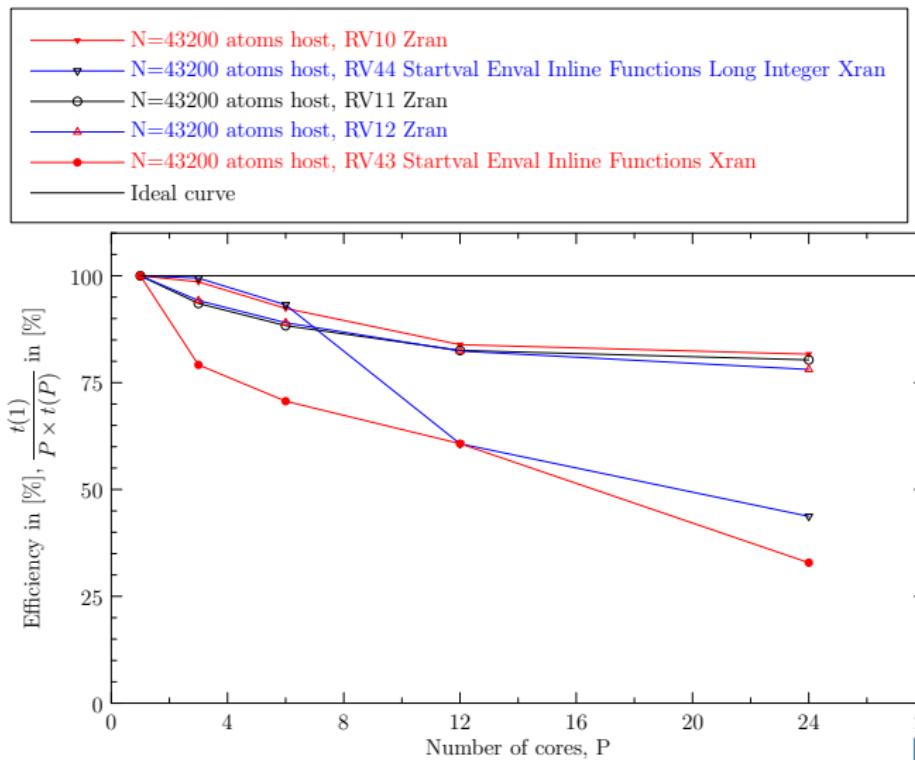
# Speedup and efficiency on computing server

Speedup plot using Precision T7810-Intel Xeon E5-2670v3 (2×12C. 2.3GHz. 30Mo cache. 2133 Mhz)



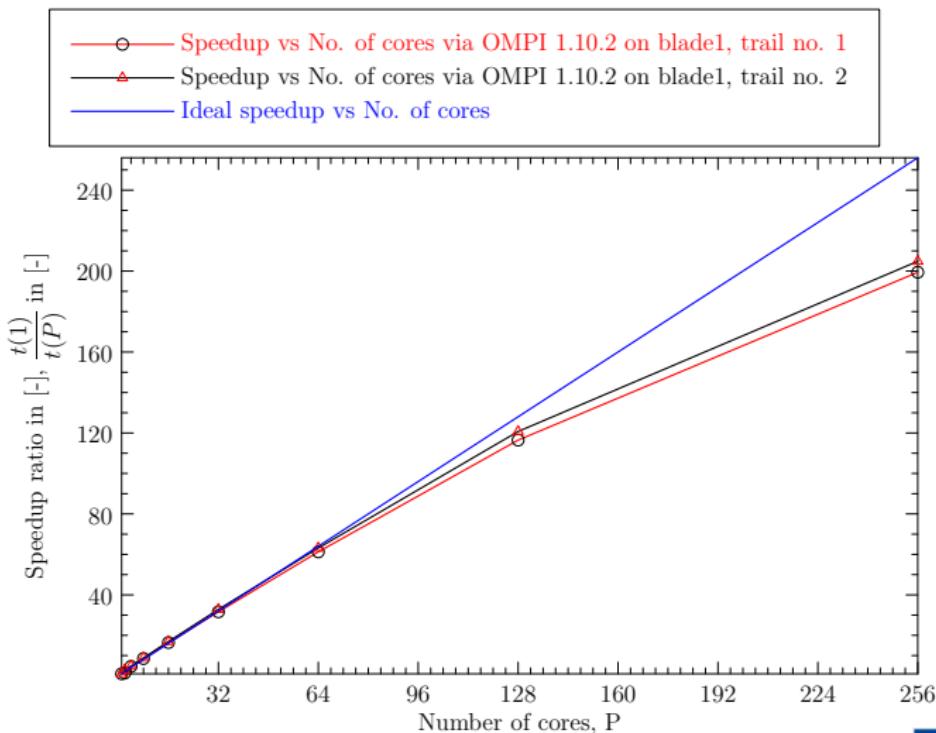
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Efficiency plot using Precision T7810-Intel Xeon E5-2670v3 (2×12C. 2.3GHz. 30Mo cache. 2133 Mhz)



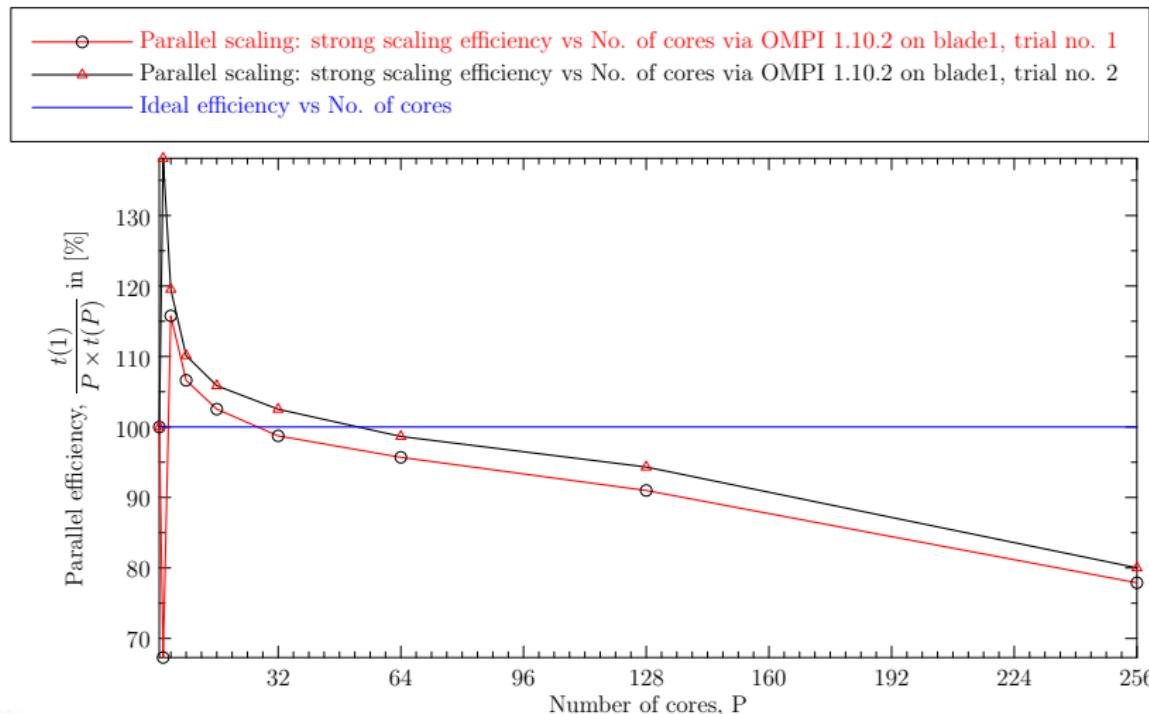
# Speedup and efficiency on CCSC (Blade1, Blade2 & defq)

Speedup plot - Distributed Memory



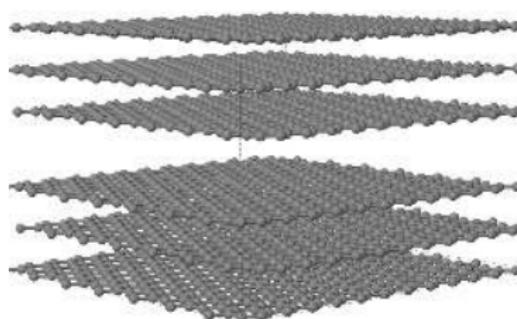
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Efficiency plot - Distributed Memory

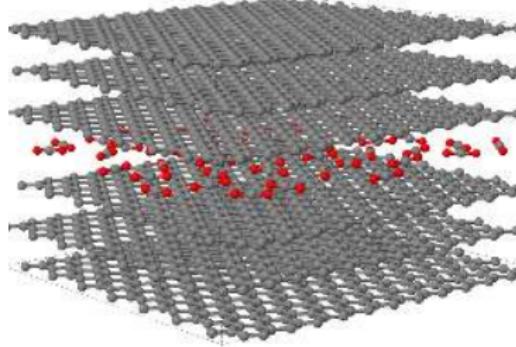


# GCMC adsorption outcomes

Adsorption of CO<sub>2</sub> through slit-like carbon structures



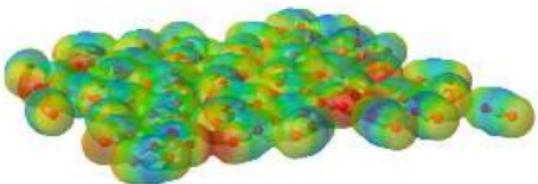
(a) Slit-like structure.



(b) CO<sub>2</sub> molecules adsorption snapshot.



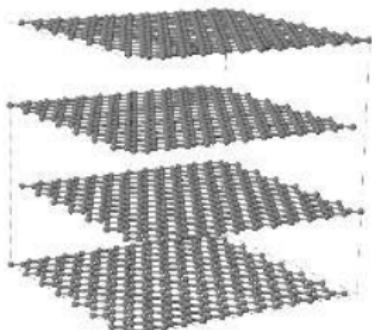
(c) CO<sub>2</sub> molecules excluding electrostatic charges. (d) CO<sub>2</sub> molecules including electrostatic charges.



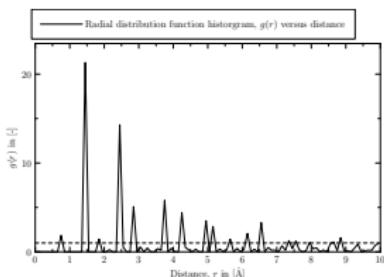


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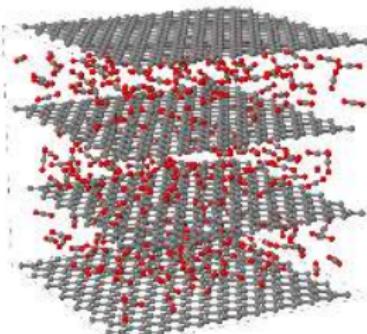
Adsorption of CO<sub>2</sub> through so-called turbostratic carbon structures



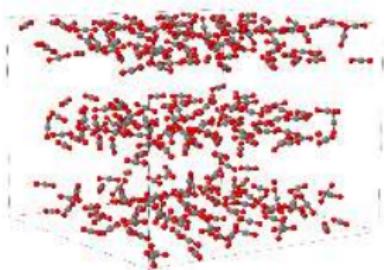
**(a)** Turbostratic structure.



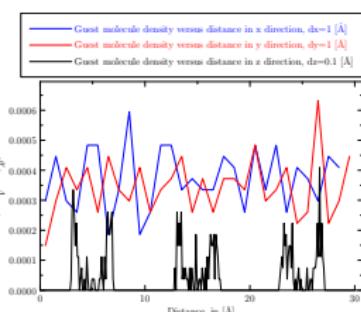
**(b)** Radial distribution function [Kouetcha et al., 2017].



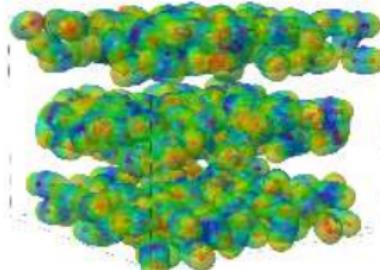
**(c)** CO<sub>2</sub> molecules adsorption.



**(d)** CO<sub>2</sub> molecules excluding electrostatic charges.



**(e)** Density profiler of CO<sub>2</sub> molecules.

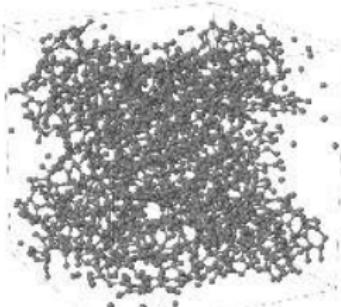


**(f)** CO<sub>2</sub> molecules including electrostatic charges.

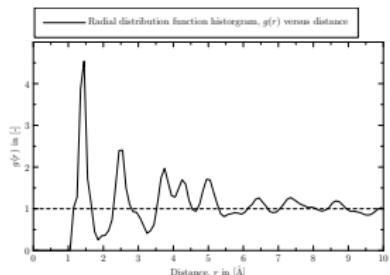


# GCMC adsorption outcomes

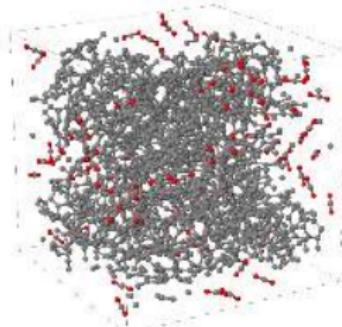
Adsorption of CO<sub>2</sub> through Activated carbon [Pikunic et al., 2003]



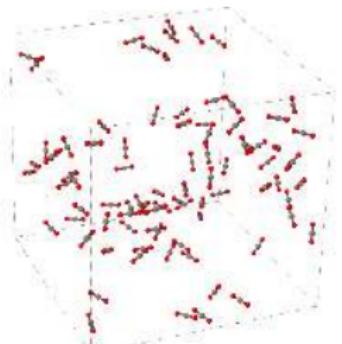
**(a)** Activated carbon.



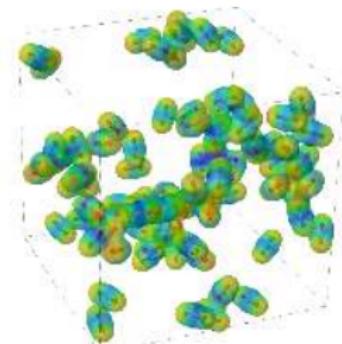
**(b)** Radial distribution function.



**(c)** CO<sub>2</sub> molecules adsorption.



**(d)** CO<sub>2</sub> molecules excluding electrostatic charges.



**(e)** CO<sub>2</sub> molecules including electrostatic charges.

## 1 Short presentation of ICMN formerly known as CRMD

### 2 Problem statement

- What are the micropollutants?
- What is the adsorption process of the micro-pollutants?
- What is the most appropriate method in modeling of the adsorption phenomenon?

### 3 Molecular simulation : Grand Canonical Monte Carlo (GCMC)

- GCMC algorithm
- Where is the bottleneck of GCMC computations?

### 4 Parallel algorithm paradigms

- First paradigm: Energy subroutine is only parallelized
- Second paradigm: Virtual volume concept
- Speedup and efficiency
- CO<sub>2</sub> adsorption outcomes

### 5 Conclusions and outlooks

- Conclusions



outlooks

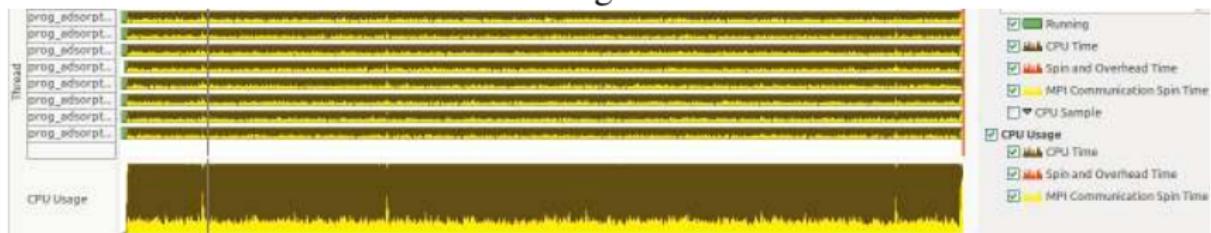


# Comparison between two algorithms

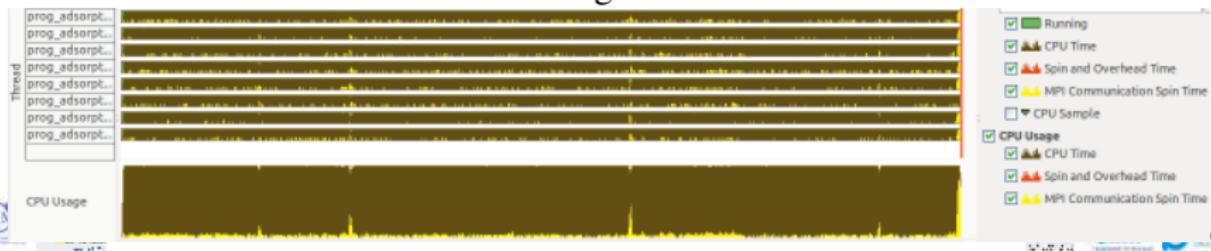
## Parallel optimization

- The nearly linear scalable plots for the paradigm 2 rely on two facts:
  - 1 MPI communications are likely less than the first algorithm,
  - 2 Serial program runtime is less than the first algorithm using the virtual volumes or so-called copied volumes.
  - 3 As a result, the program runtime on single core over MPI communications ratio is fairly optimized.

Paradigm 1



Paradigm 2

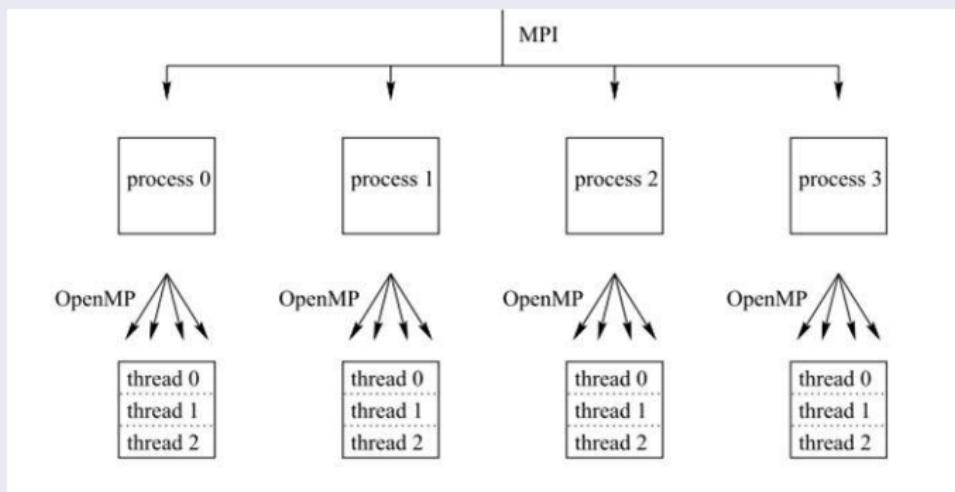


# Further speedup

Hybrid MPI-OMP programming??

## 1 Hybrid MPI/OpenMP programming.

- MPI does inter-node computations (distributed memory computation),
- OpenMP performs the computations on the available threads (shared memory computation)



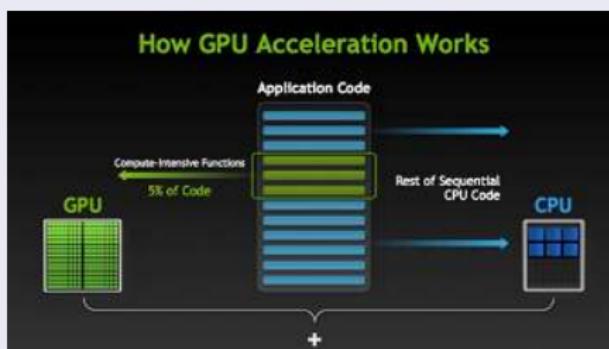
## Further speedup

## GPU computing

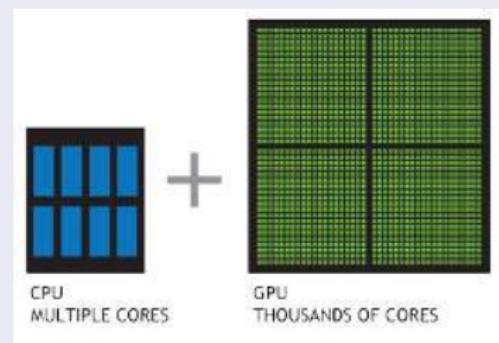
<http://www.nvidia.com/object/what-is-gpu-computing.html>

## GPU computing

- Cuda C programming [Cheng et al., 2014; Sanders and Kandrot, 2010],
  - OpenCL programming.



**(a) How GPUs accelerate software applications.**



(b) Thousands of cores

# Further speedup

GPU supercomputing data extracted from "<https://www.top500.org/lists/2017/11/>"

## TOP 5 list of the fastest supercomputers in the world (November 2017)

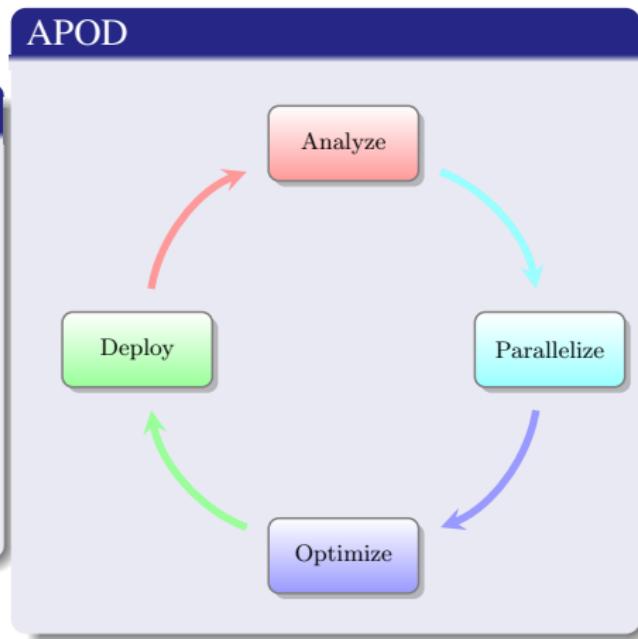
Rank	System	Cores	Rmax [TFlop/s]	Rpeak [TFlop/s]	Power [kW]
1	Sunway TaihuLight - Sunway MPP, Sunway SW26010 260C 1.45GHz, Sunway , NRCPC National Supercomputing Center in Wuxi China	10,649,600	93,014.4	125,435.9	15,371
2	Tianhe-2 [MilkyWay-2] - TH-IVB-FEP Cluster, Intel Xeon E5-2692 12C 2.20GHz, TH Express-2, Intel Xeon Phi 31S1P , NUOT National Super Computer Center in Guangzhou China	3,120,000	33,862.7	54,902.4	17,808
3	Piz Daint - Cray XC50, Xeon E5-2690v3 12C 2.6GHz, Aries interconnect, NVIDIA Tesla P100 , Cray Inc. Swiss National Supercomputing Centre (CSCS) Switzerland	361,760	19,590.0	25,326.3	2,272
4	Gyoukou - ZettaScaler-2.2 HPC system, Xeon D-1571 16C 1.0GHz, Infiniband EDR, PEZY-SC2 700MHz , ExaScaler Japan Agency for Marine-Earth Science and Technology Japan	19,860,000	19,135.8	28,192.0	1,350
5	Titan - Cray XK7, Opteron 6274 16C 2.20GHz, Cray Gemini interconnect, NVIDIA K20x , Cray Inc. DOE/SC/Oak Ridge National Laboratory United States	560,640	17,590.0	27,112.5	8,209



# REAL speedup

## Basic rules for real speedup and APOD

- 1 Think parallel and design parallel algorithms (CB-GCMC, AI ...)
- 2 Use the basic rules of optimizations,
- 3 Profiling (serial code) and parallel code profiling,
- 4 Micro-optimizations,
- 5 Minimizing the amount of time spent on memory.



# *Acknowledgments*

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# *Questions?*



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